

# Andreas Lyng

## Verified computer algebra in homotopy type theory

- Build a homotopy type theoretic algebra library
- Apply novelties of homotopy type theory:
  - Univalence axiom
  - Higher inductive types
- Computer verify correctness of algorithms in algebra
- Develop techniques to obtain efficient algorithms



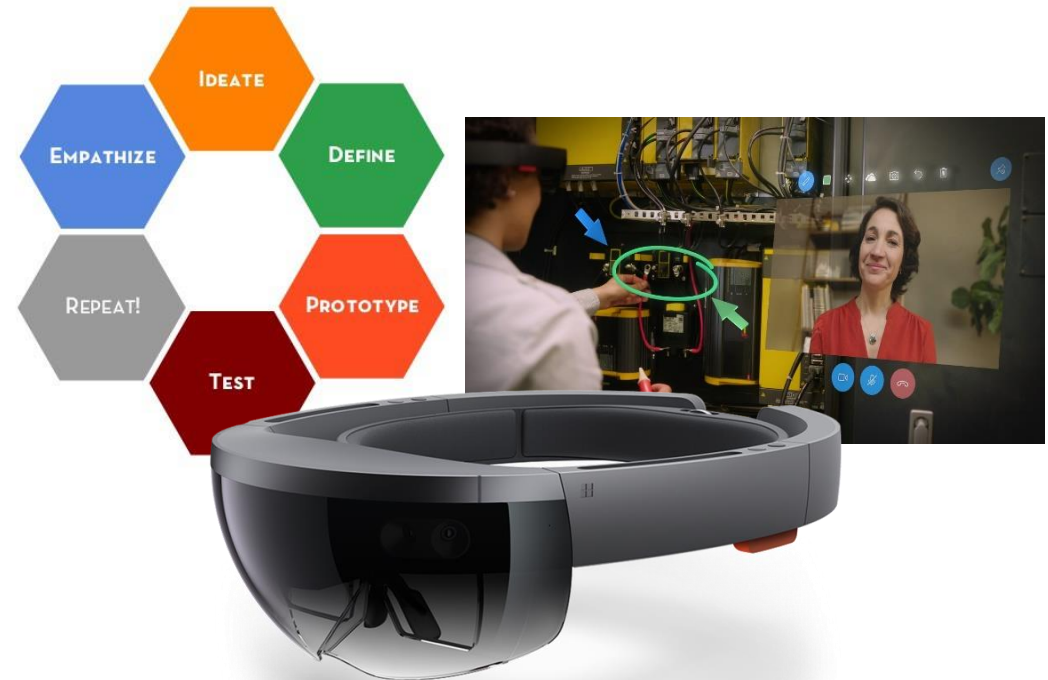
# AR-based Interaction Techniques for Remote Assistance

*Troels A. Rasmussen – UbiComp Group*

I conduct empirical studies of current practices in industry. Cases include LEGO and Vestas.

I develop AR-prototypes for remote assistance.

I study the effects of different interaction techniques on the performance, process and satisfaction of remote assistance. In the lab and in the field.



# DETECTING SELECTION USING DEEP LEARNING

BAKHTAWAR NOOR

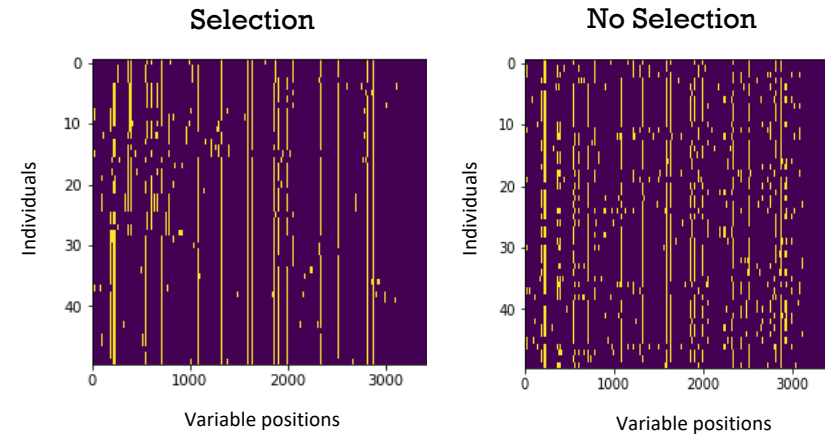
## Introduction

- Selection leaves patterns of genetic variation in the DNA
- **Goal:** Detect these patterns of genetic variation a.k.a selection given some input matrix

## Method

- **Tool:** Convolution neural network
  - Why? They are good at handling high dimensional

## Data



## Input:

- Input is a 2D matrix filled with 0s' and 1s'.
- **Rows** in the matrix are individuals
- **Columns** are variable positions among individuals

# Verifiable cryptographic software

The goal of my PhD research is to develop a formally verified library of cryptographic software.

Focus will be on elliptic curve cryptography including

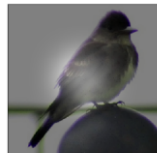
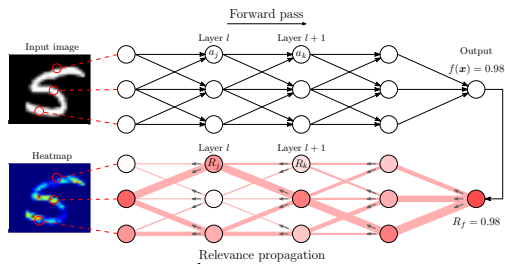
- Implementing concrete curves and their group operation.
- Provide a general library for elliptic curve cryptography.
- Pairing-based elliptic curve cryptography including implementations of pairing algorithms and pairing-friendly curves.

Challenges include

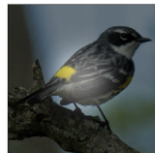
- Implementations must be timing-attack resistant.
- Achieving performance which is comparable to unverified implementations.
- Achieving both good performance and security.

# Fast, effective and interpretable Deep Learning

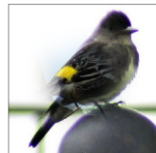
- ▶ What input features were salient for a given prediction?
- ▶ How should I change a given input to make the network “choose” another class?



Olive sided Flycatcher



Myrtle Warbler



*Current approach:* Invertible neural networks

# Anonymous Information Flow

## Motivating example: Simple auction with three users

- Bidding according to secret strategies
  - *Cat* follows strategy  $\varphi$
  - *Dog* follows strategy  $\psi$
  - *Fish* follows strategy  $\vartheta$
- Can the highest bid be publicly disclosed without disclosing who won?
  - Does depend on secrets so violates Non-Interference
  - ...yet, information disclosed is 'symmetric' in the users

## Capturing the symmetry:

- Poirot thinks possible



- ⇒ Poirot thinks possible



- Gives bound on Poirot's knowledge s.t. composition preserves symmetry

Who used  $\varphi$ ?  
I shall use my  
little grey cells!

$$\frac{\omega(\text{Cat}) = \omega'(\text{Dog}) \quad \omega(\text{Dog}) = \omega'(\text{Cat}) \quad \omega(\text{Fish}) = \omega'(\text{Fish})}{\omega \sim_{\text{Cat, Dog}} \omega'}$$

$$\forall \omega, \omega': \omega \sim_{\text{Cat, Dog}} \omega' \wedge \omega \in k \Rightarrow \omega' \in k$$

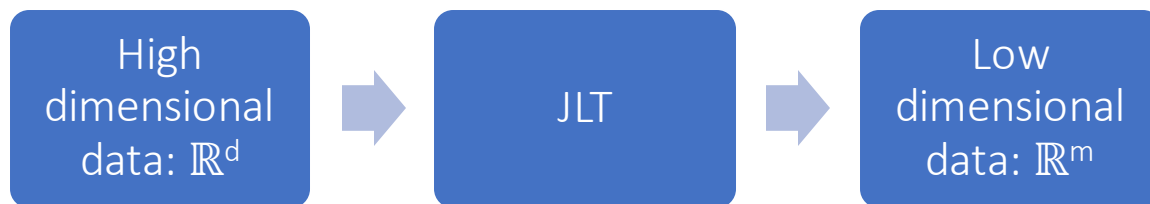


Extra Details

Handwritten mathematical notes and formulas:

- $(M, s) \in K_i \varphi \Rightarrow (M, s') \in \varphi$
- $(M, s) \in K_i \psi \Rightarrow (M, s') \in \psi$
- $(M, s) \in K_i \vartheta \Rightarrow (M, s') \in \vartheta$
- $(M, s) \in K_i \varphi \wedge (M, s) \in K_i \psi \Rightarrow (M, s') \in K_i \varphi \wedge (M, s') \in K_i \psi$
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# "Basic" Introduction to Johnson-Lindenstrauss Transforms (JLTs)



$$m = O(1/\epsilon^2 \cdot \log(1/\delta))$$

$\delta$ : The JLT is allowed to fail with probability  $1 - \delta$

$\epsilon$ : The  $\ell_2$  norm of the embedded datum is within  $(1 \pm \epsilon)$  of the original  $\ell_2$  norm

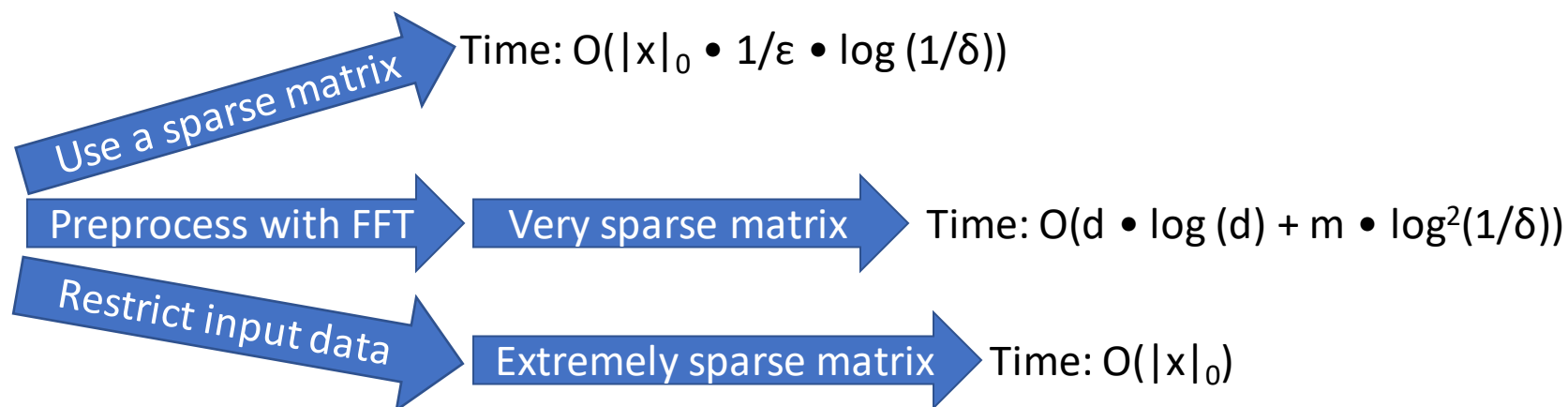
$m$  does not depend on  $d$ !

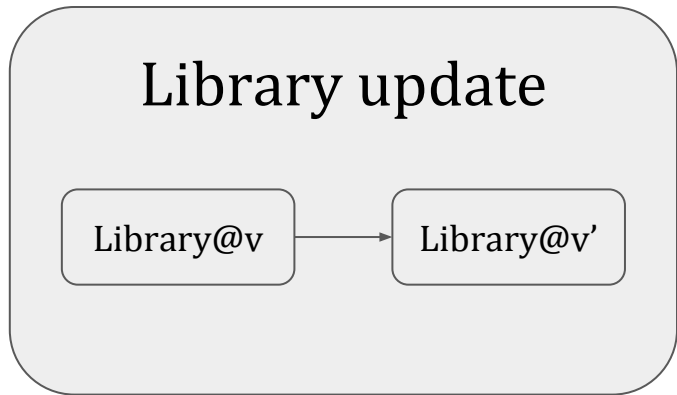
An example JLT:

An  $m \times d$  matrix, where each entry is i.i.d. sampled from  $\pm 1$ .

Time to apply this JLT:  $O(d \cdot m)$  or  $O(|x|_0 \cdot m)$

Are there faster JLTs?





Non-breaking ✓



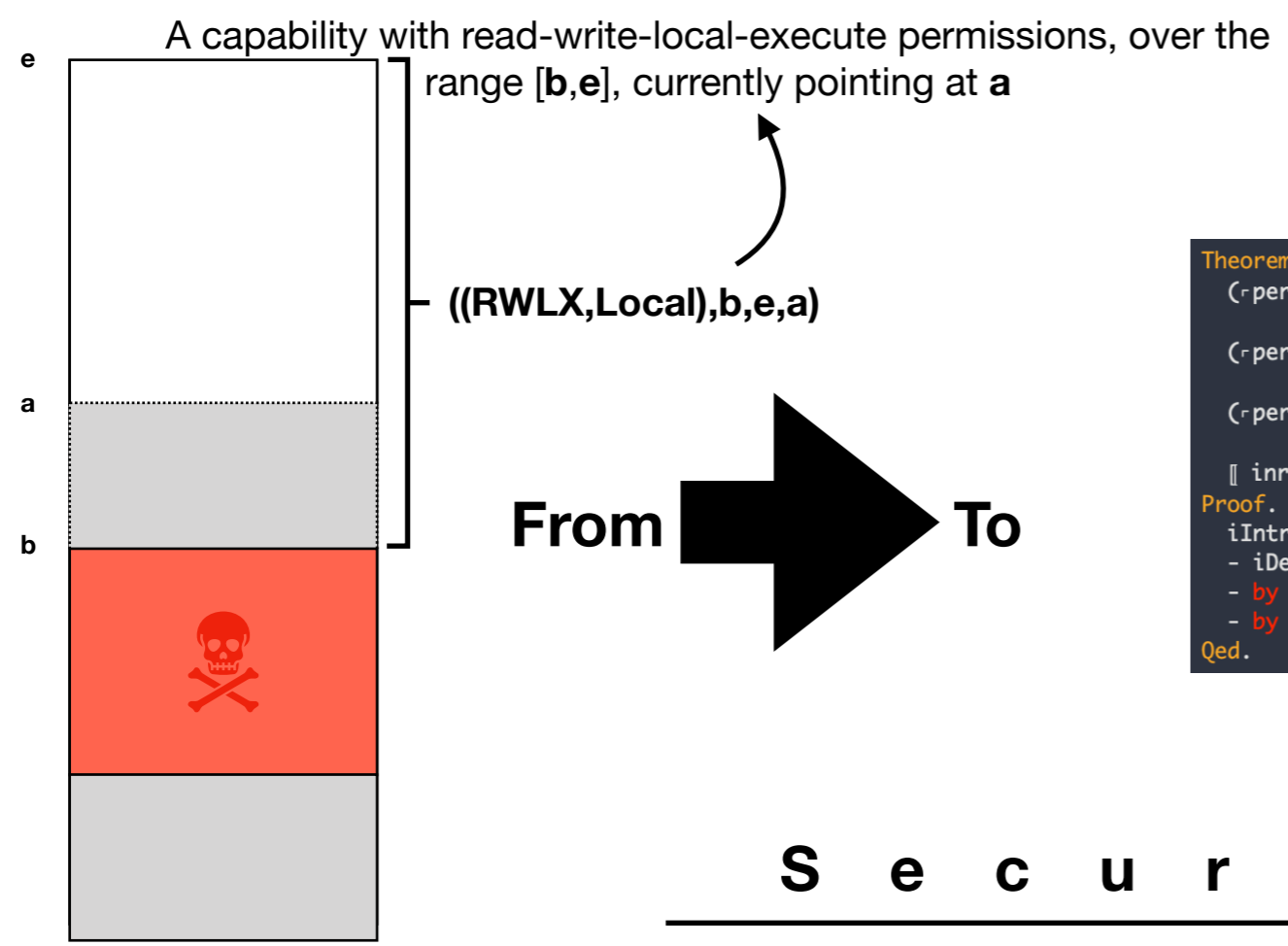
Breaking ✗





# Reasoning about capability machines in Iris, a higher-order concurrent separation logic framework

Capability: unforgeable token of authority

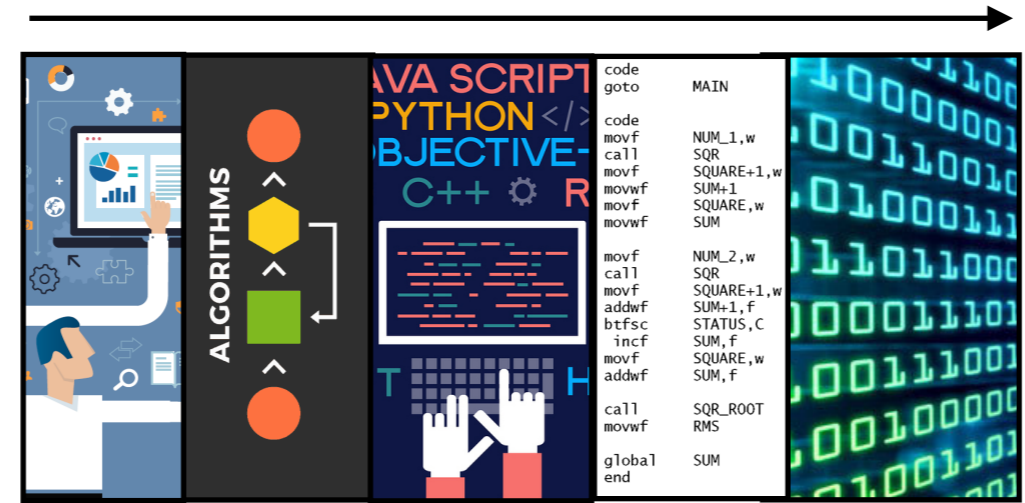


```
Theorem fundamental (perm : Perm) b e g (a : Addr) stsf E r :
  (¬perm = RX¬ ∧ (∃ ws, [* list] a; w ∈ (region_addrs b e); ws, na_inv logrel_nais (logN .@ a)
    (read_only_cond a w interp))) v
  (¬perm = RWX¬ ∧ ([* list] a ∈ (region_addrs b e), na_inv logrel_nais (logN .@ a)
    (read_write_cond a interp))) v
  (¬perm = RWLX¬ ∧ ([* list] a ∈ (region_addrs b e), na_inv logrel_nais (logN .@ a)
    (read_write_local_cond a interp))) -*
  [[ inr ((perm,g),b,e,a) ]]_e stsf E r.
Proof.
iIntros "[#[-> Hinv] | #[-> Hinv] | #[-> Hinv]]".
- iDestruct "Hinv" as (ws) "Hinv". by iApply fundamental_RX.
- by iApply fundamental_RWX.
- by iApply fundamental_RWLX.
Qed.
```

Formalized proofs in Iris

Capability Machine model

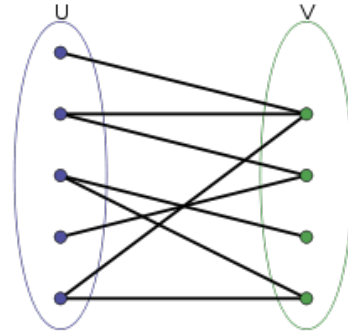
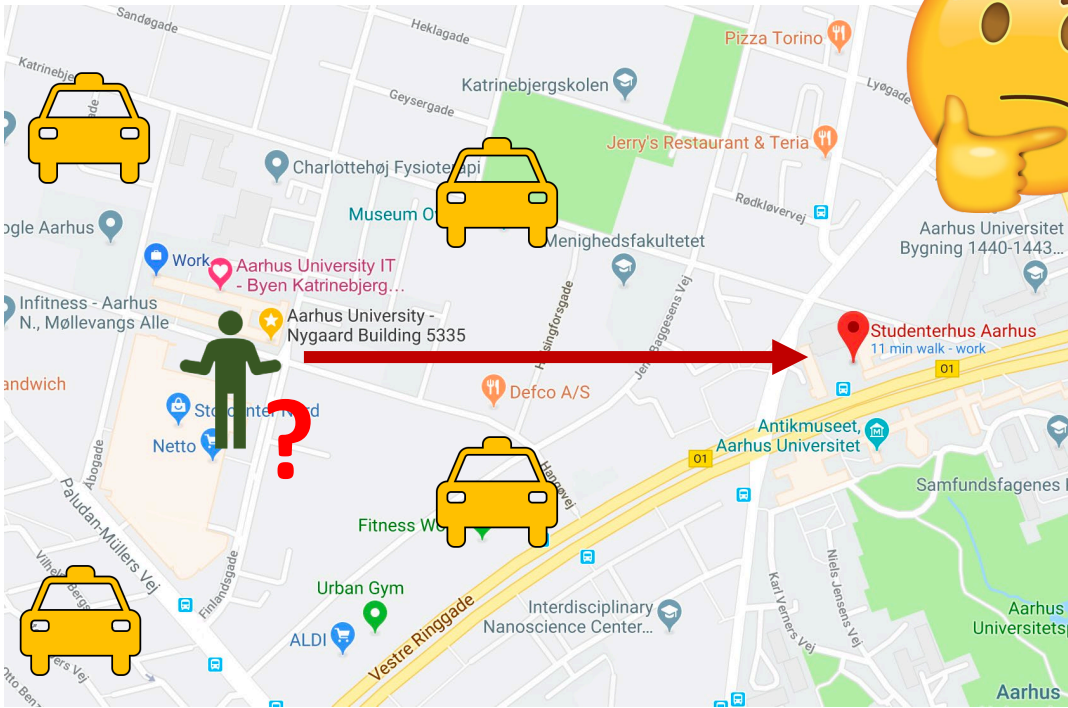
S e c u r i t y



Abstraction Layers

**Goal:** a compiler that *provably* preserves the security properties of a high level source language

# Substantial Taxi Service



$$P_{qk}(r_{+1}) = P_{qkr} \cdot (F_k \cdot F'_{kl} + (1 - F_k) \cdot \pi_{kl}) \quad (2)$$

where  $\cdot$  is a dot product, and

$$F_k = \frac{\mathbb{E}[\sum_l C_{klr}]}{\sum_q P_{qkr}} \quad (3)$$

$$F'_{kl} = \left(1 - \prod_{kl} Pr_{klr}(0)\right) \cdot \frac{\mathbb{E}[C_{klr}]}{\mathbb{E}[\sum_l C_{klr}]} \quad (4)$$

The lemma with Eq. 4 can be found in the appendix. We use  $Pr_{klr}(x)$  to estimate the expected value of  $C_{klr}$ , and we model  $Pr_{klr}(x)$  as a Poisson distribution with mean  $\lambda_{klr}$ :

$$Pr_{klr}(x) = e^{-\lambda_{klr}} \frac{\lambda_{klr}^x}{x!}$$

We adapt a method of Multiple Random Walkers [8] in order to calculate  $p_{qk}$ . Assume a set of drivers are random walkers that restart at each walking step to a new location. The new location is selected randomly for each walker according to the probability distribution  $r_{kl}^r, \sum_l r_{kl}^r = 1$ . We initialize  $r_{kl}^r$  as

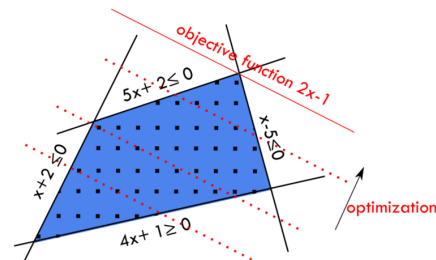
$$= \frac{1}{N}$$

1)  $p_{qkr}$  at the same time:

$$\delta) r_{kl}^r + \delta \Phi_r \quad (5)$$

$$: p_{qkr} \cdot r_{kl}^r \quad (6)$$

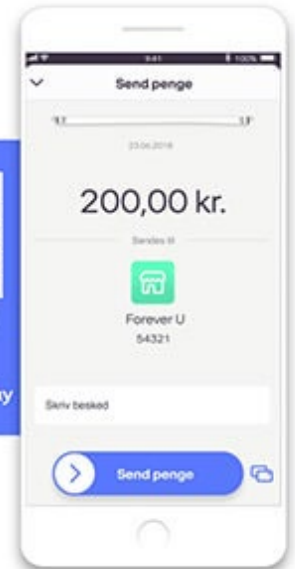
Eq. 2:



optimization

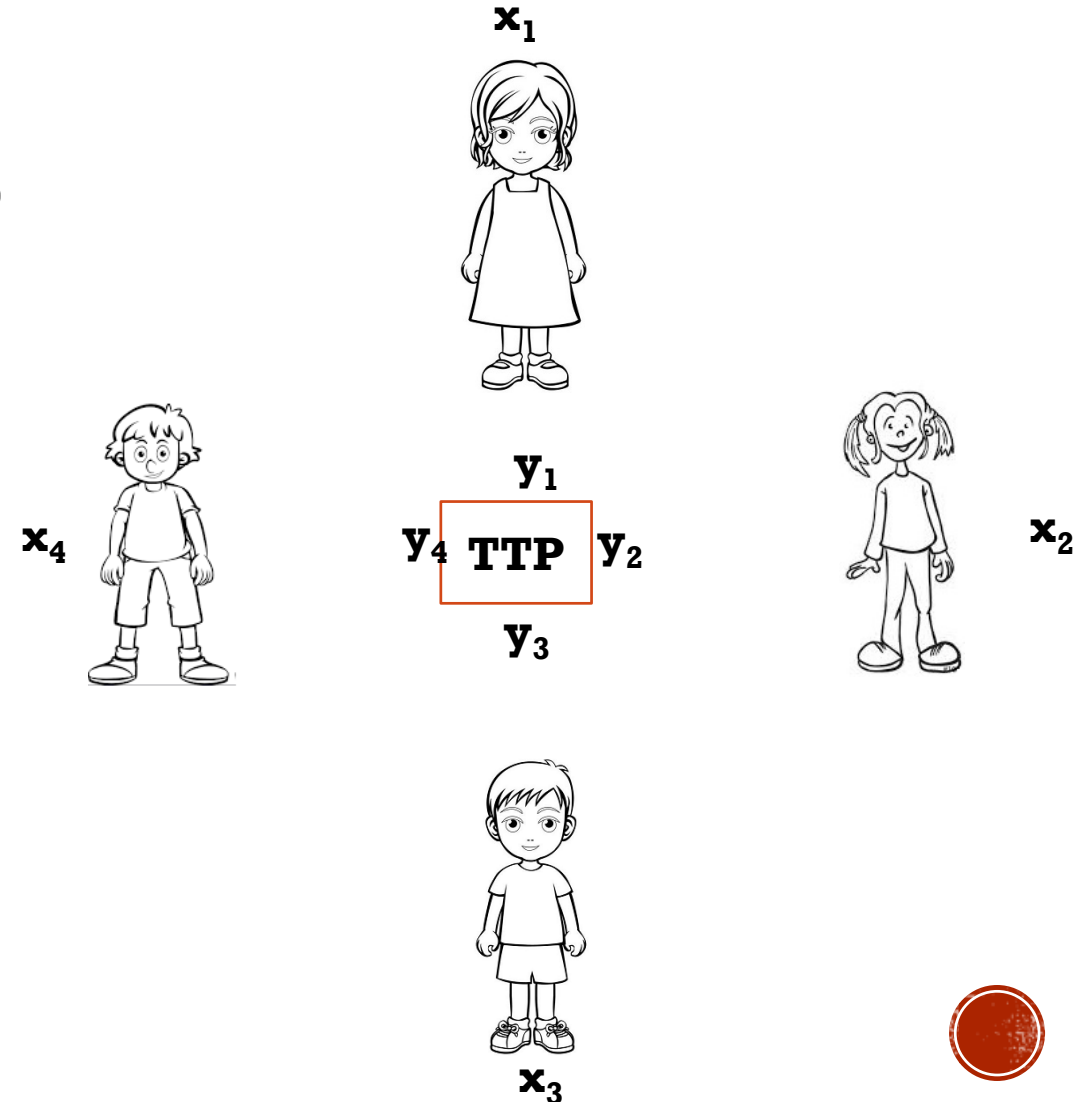
K-Means clustering

Hierarchical clustering



# SECURE MULTI-PARTY COMPUTATION (MPC)

- Parties with **private** inputs
- **Goal:** Compute **joint** function  $f(x_1, x_2, x_3, x_4)$
- **Mutual distrust**
  - Adversary corrupts  $t$  out of  $n$  parties
- Two important requirements
  - Privacy
  - Correctness
- MPC emulates TTP
- TTP – Trusted Third Party

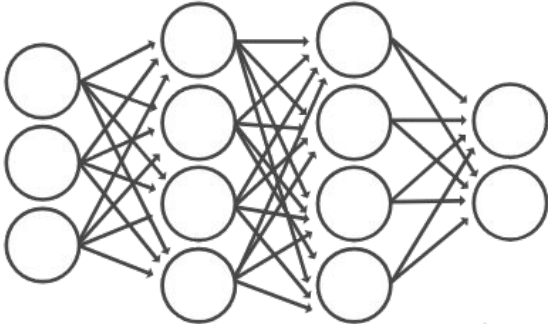


# FieldAI

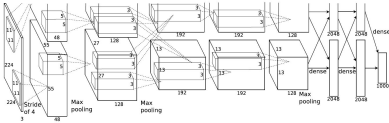


+

deep learning



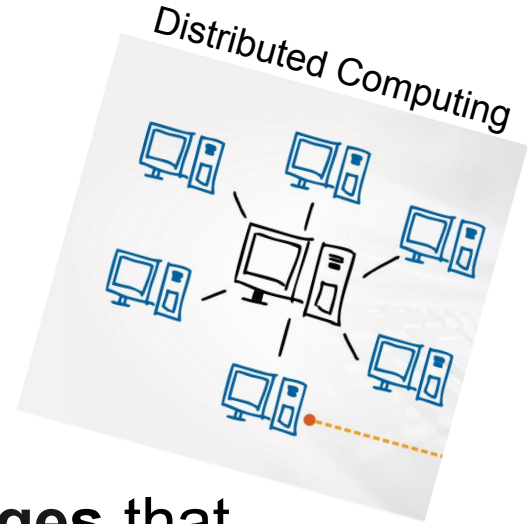
=



?

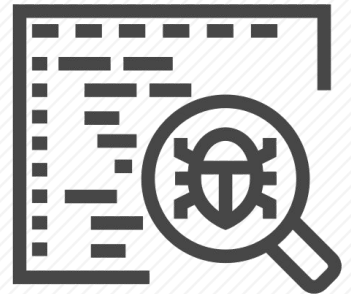
$x \in \{ \text{multispectral, SAR, height, weather, ...} \}$   
 $y \in ???$





How to design **programming languages** that **protects secret data** from being inadvertently disclosed?

$$\frac{\text{S-ASSIGN} \quad \langle e, m \rangle \Downarrow \langle v; l_e \rangle \quad pc \sqcup l_e \sqsubseteq lev(x)}{\langle x = e, m, pc \rangle \longrightarrow_{a(x,v)} \langle \text{stop}, m[x \mapsto v], pc \rangle}$$



# SINGLE CELL RNA-SEQ OF TESTIS SAMPLES

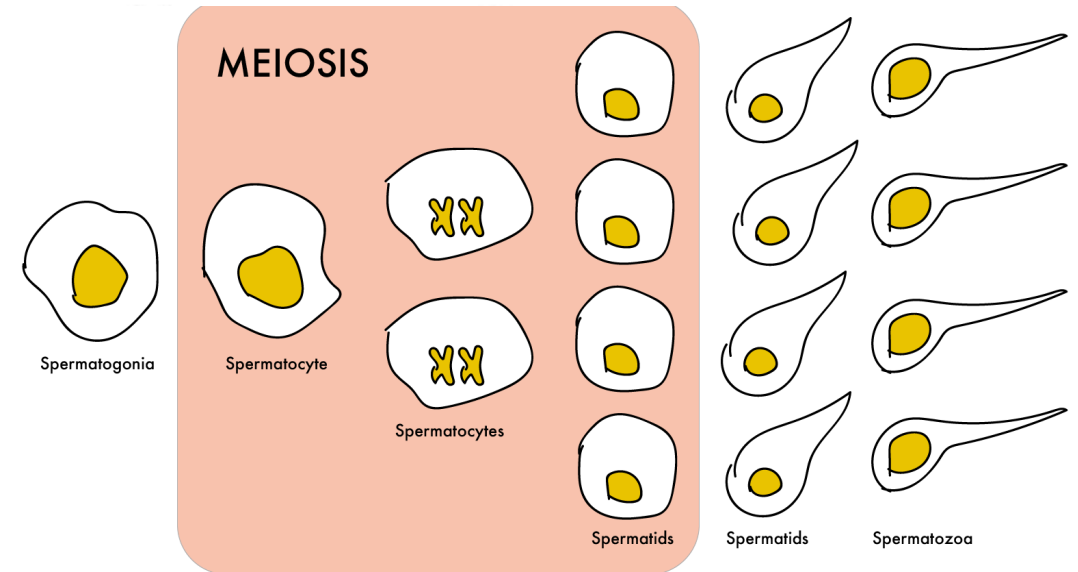
## PROBLEM

- Around 10-15% of couples are infertile
- Testicles include many cell types

## SOLUTION

- Using single cell RNA-Seq we can identify cell types
- By comparing the expression of healthy and non-healthy cell types we can extract markers for infertility
- If we have markers, we can better understand infertility and

**CURE IT**



# SINGLE CELL RNA-SEQ OF TESTIS SAMPLES

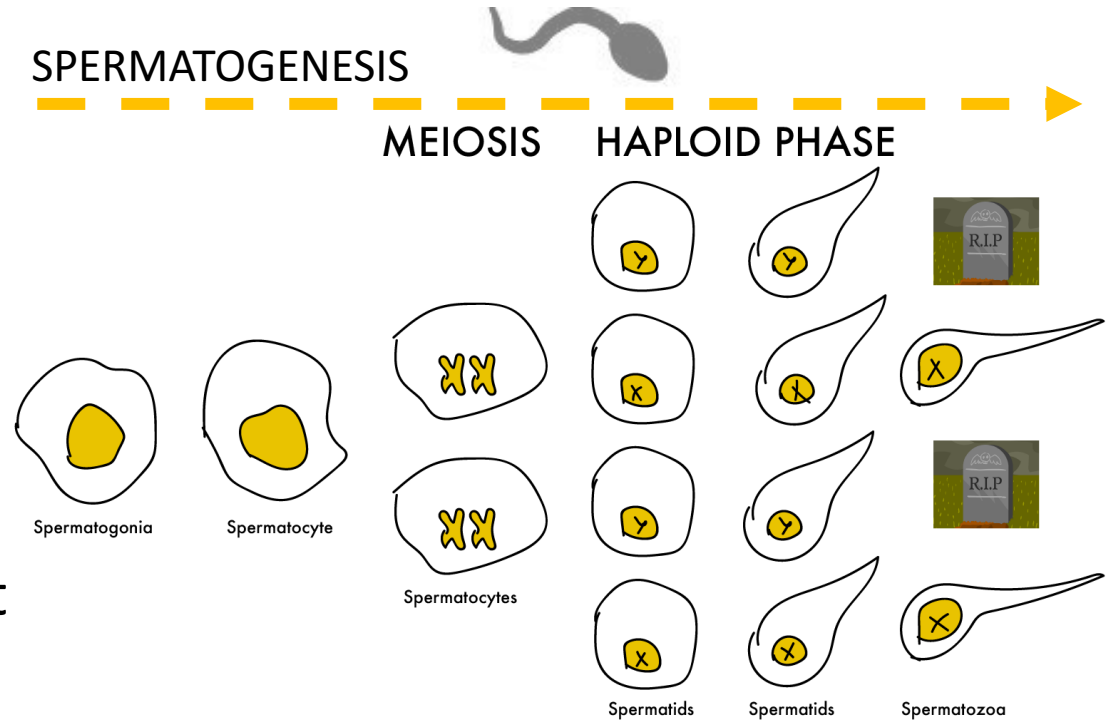
## HYPOTHESIS

The X and Y chromosomes have been fighting a war during the evolution of our species

## SCIENTIFIC DESIGN'S MAIN IDEAS

- The battle ground is spermatogenesis
- After meiosis, the battle begins
- Using single cell sequencing, we can target cell types
- By analyzing the expression in the haploid phase, we can detect signs of past fights
- We can better understand the complex evolutionary history of our sex chromosomes

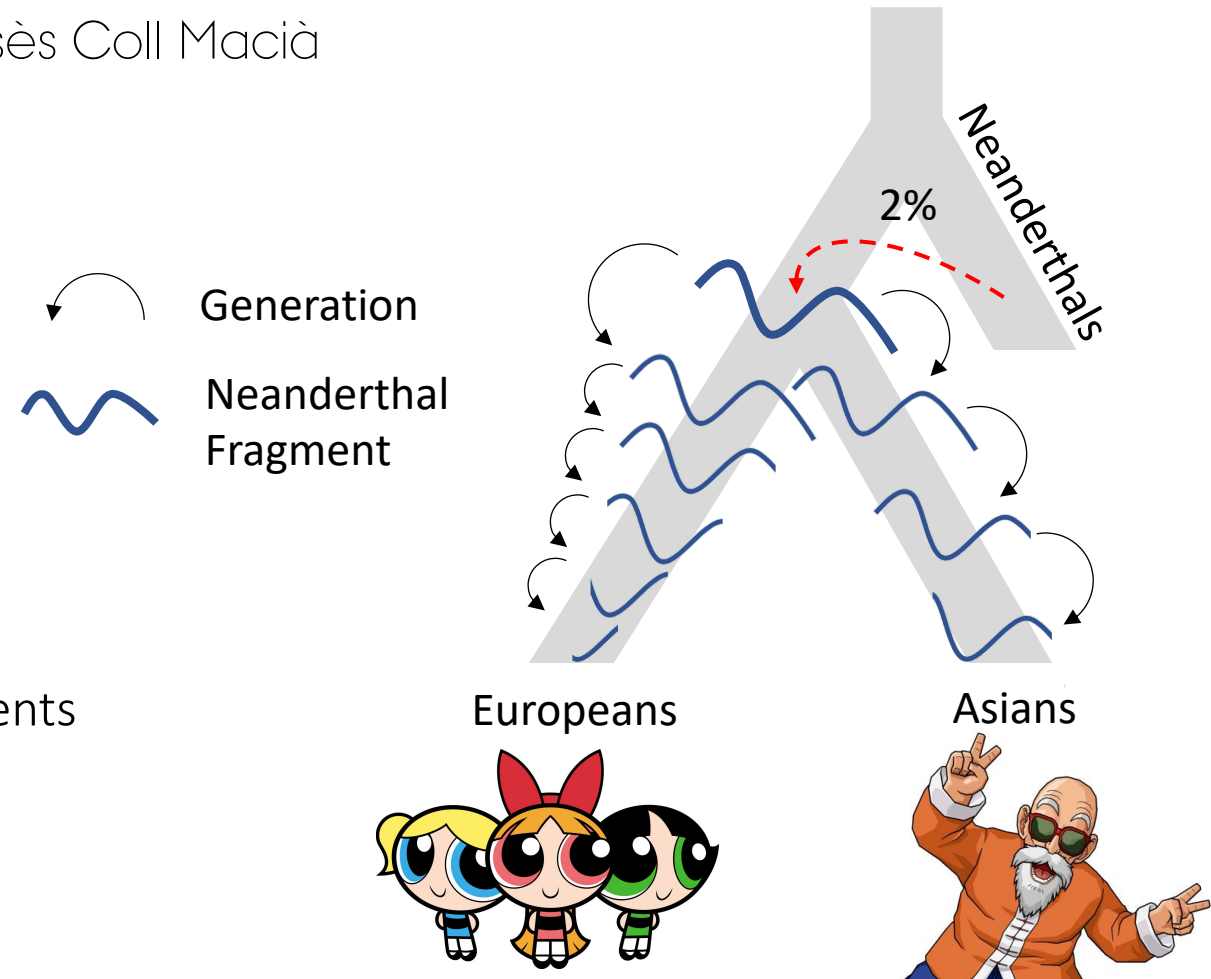
## SPERMATOGENESIS



# Generation time differences between Europeans and Asians inferred by Neanderthal fragment length

Moisès Coll Macià

- 2% of our DNA comes from Neanderthals
- Each generation DNA fragments shorten
- The more generations, the shorter the fragments are
- We find:
  - Europeans have short fragments
  - Asians have long fragments
- Thus, Europeans must have had younger parents than Asians during the last 50,000 years



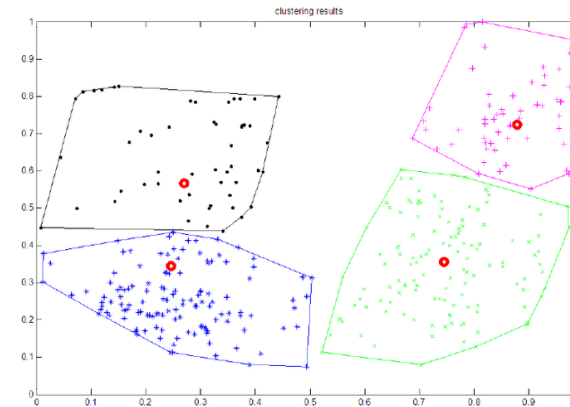
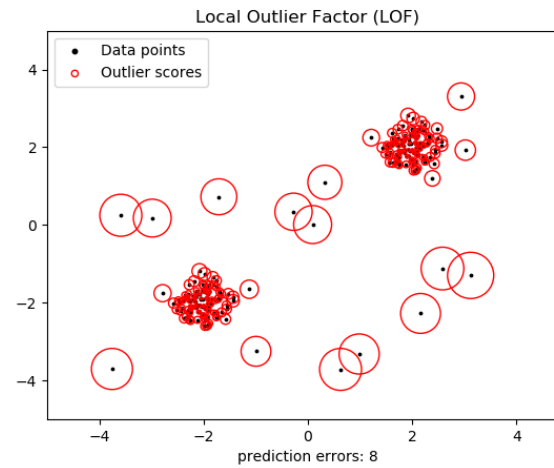
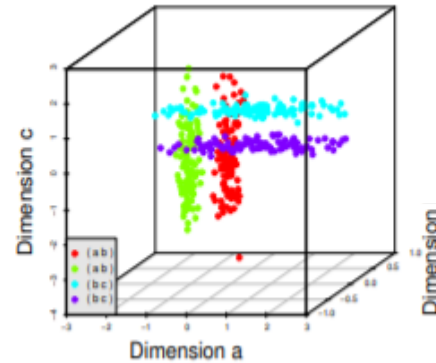


# Data Science on the Desktop

## - Data Mining on Modern Hardware

Exploit multi-core CPUs and GPUs to speed up Data Mining tasks, such as

- Clustering
- Outlier Detector
- Trend Detection
- ...



Identify suitable task for GPU and CPU

Standard C Code

```
void saxpy(int n, float a,
          float *x, float *y)
{
    for (int i = 0; i < n; ++i)
        y[i] = a*x[i] + y[i];
}

int N = 1<<20;

// Perform SAXPY on 1M elements
saxpy(N, 2.0, x, y);
```

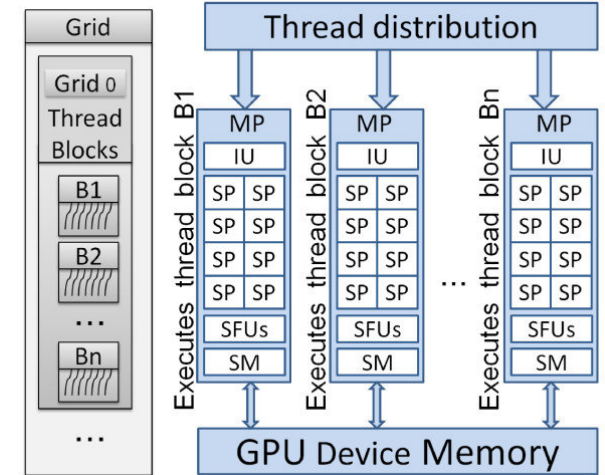
C with CUDA extensions

```
__global__
void saxpy(int n, float a,
          float *x, float *y)
{
    int i = blockIdx.x*blockDim.x + threadIdx.x;
    if (i < n) y[i] = a*x[i] + y[i];
}

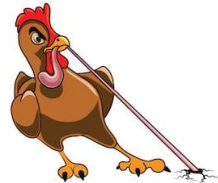
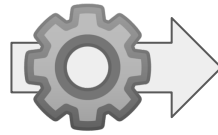
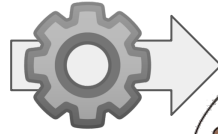
int N = 1<<20;
cudaMemcpy(x, d_x, N, cudaMemcpyHostToDevice);
cudaMemcpy(y, d_y, N, cudaMemcpyHostToDevice);

// Perform SAXPY on 1M elements
saxpy<<<4096,256>>>(N, 2.0, x, y);

cudaMemcpy(d_y, y, N, cudaMemcpyDeviceToHost);
```



# Chickens, bugs and compilers

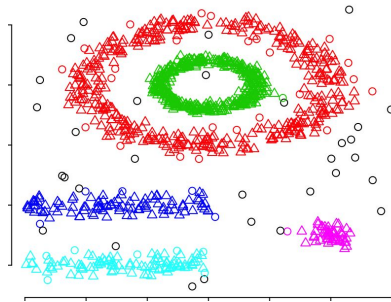


# Data Science on the Desktop

## - Data Mining on Modern Hardware

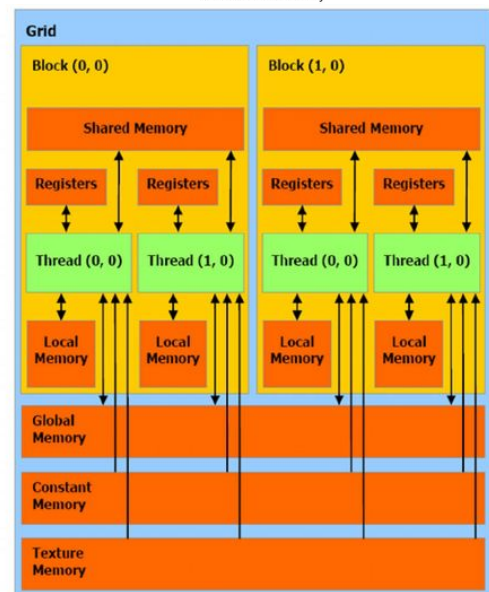
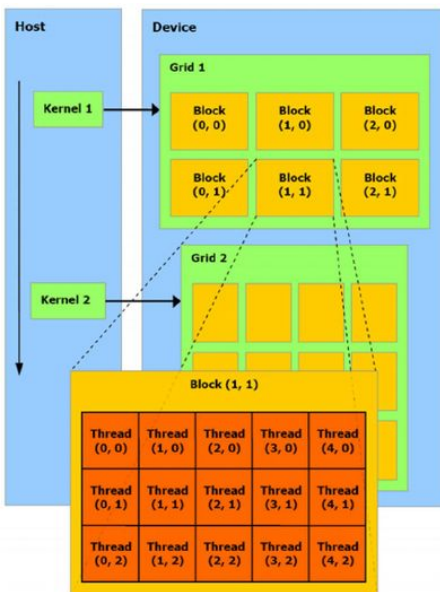
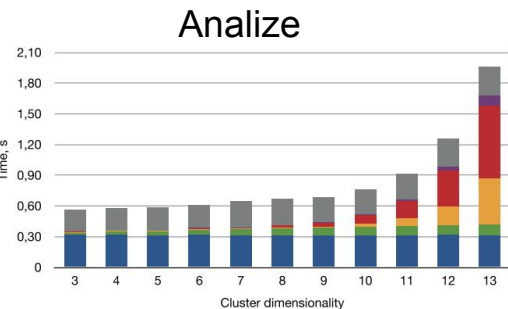
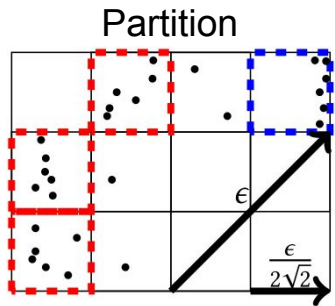
Exploding multi-core CPUs and GPUs to speed up data mining algorithms, for tasks such as:

- Clustering
- Outlier detection
- Trend detection
- ...



Identify suitable tasks for CPU and GPU

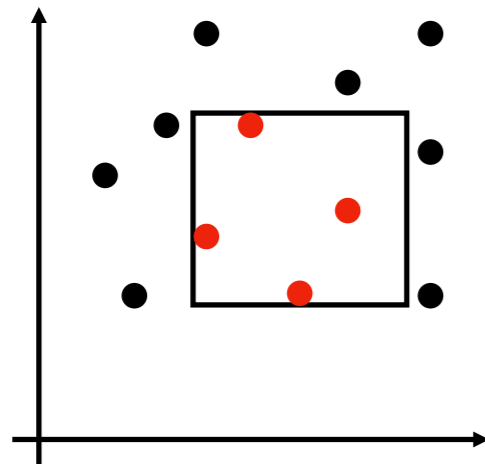
Balance throughput and data transfer



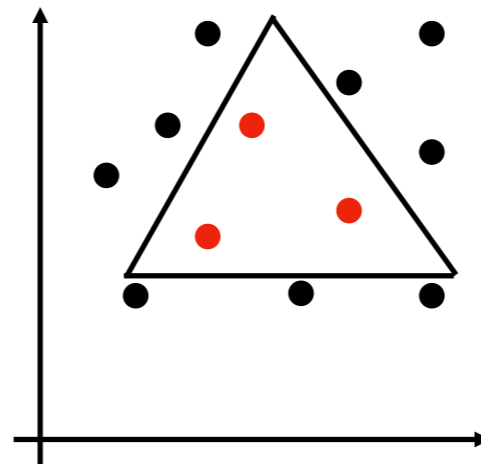


**Range Searching:** Given a set of  $n$  points in  $d$  dimensional space, we want to build a data structure such that given a query range (a subspace), we can count or report the points in the query range efficiently.

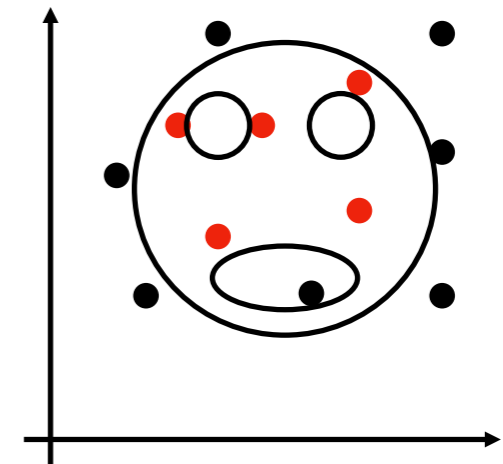
**Examples in 2D:**



**Othogonal  
Range Searching**



**Simplex  
Range Searching**



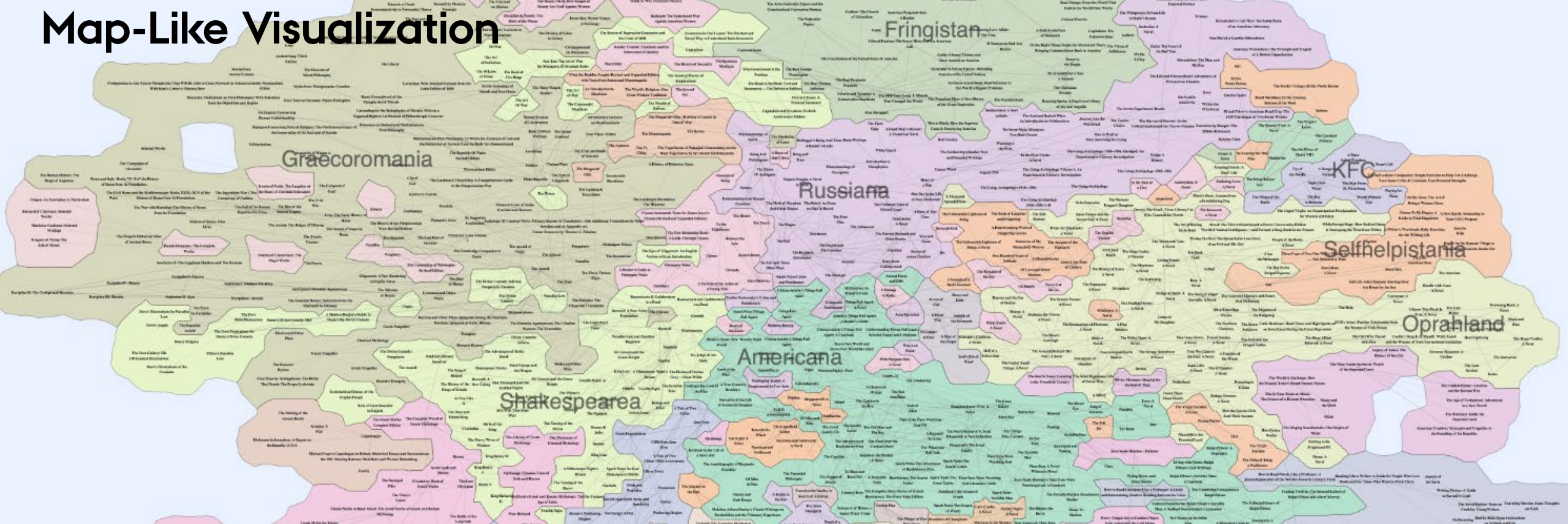
**Semialgebraic  
Range Searching**

many people engaged in many activities mediated by many artifacts. discuss.

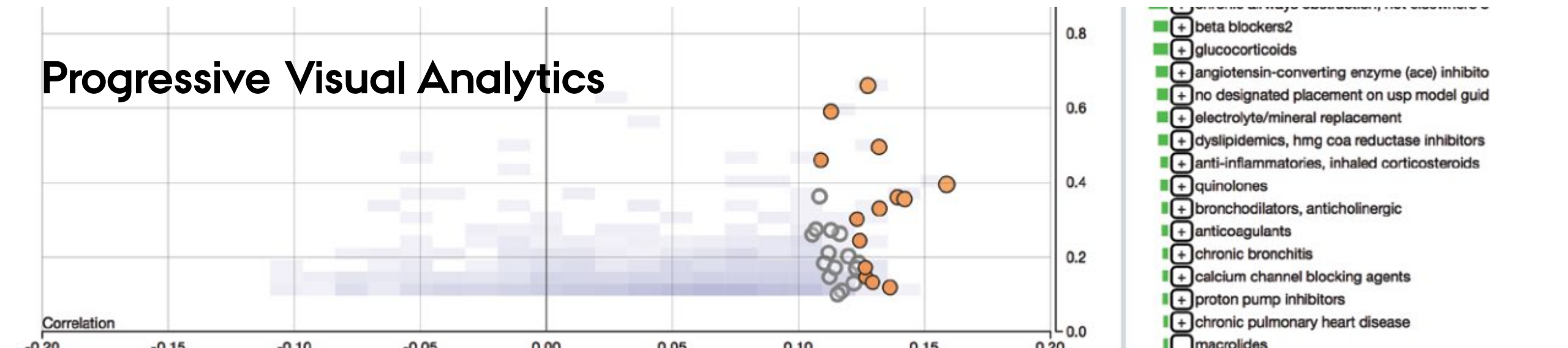
welcome to modern life  
 welcome to artifact ecologies  
 (Peter Lyle, CMA)



# Map-Like Visualization



# Progressive Visual Analytics



YOU PROBABLY CAN'T PRONOUNCE THIS



**João Belo**

Ubiquitous Computing and Interaction Group

## Context Aware User Interfaces for Augmented Reality



- Computational Interaction



"SMART" USER INTERFACES,  
OPTIMIZED DEPENDING ON  
USER NEEDS / BEHAVIOUR

- Deep Learning (ConvNets)



UNDERSTAND THE USER AND  
HIS/HER ENVIRONMENT

WE MAKE COOL STUFF! COLLABORATE WITH US!

# Privacy-Preserving Machine Learning (PPML)

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- Infeasible for consumers and companies to train complex machine learning models independently
- So machine learning as a service (MLaaS) is offered by companies such as Amazon, Google and Microsoft
- Concerns:
  - Privacy about the queries being made to the servers
  - Loss of competitive advantage due to sharing data with Amazon when performing collaborative machine learning



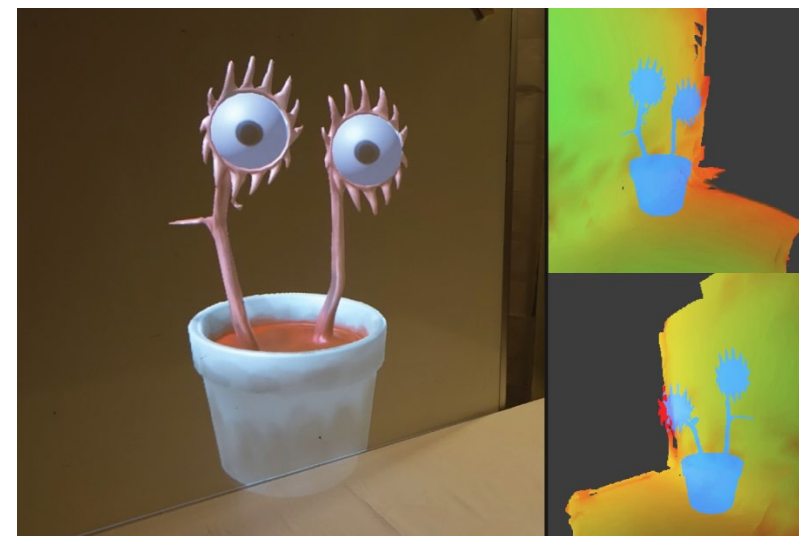
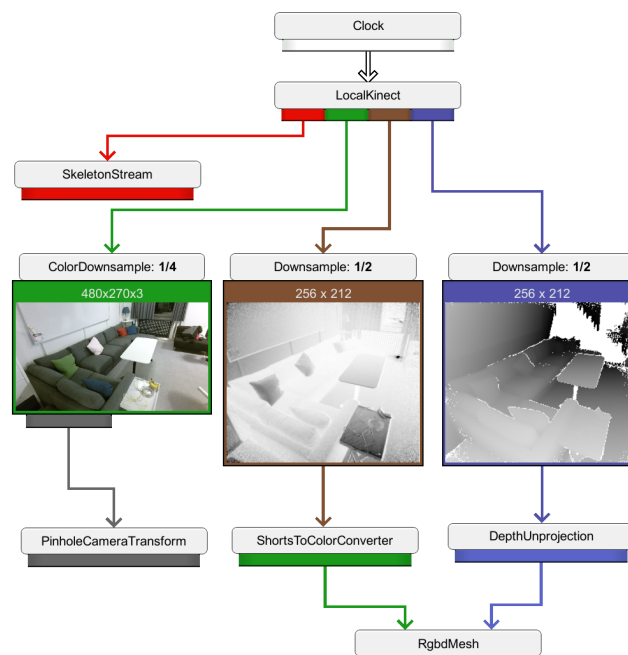
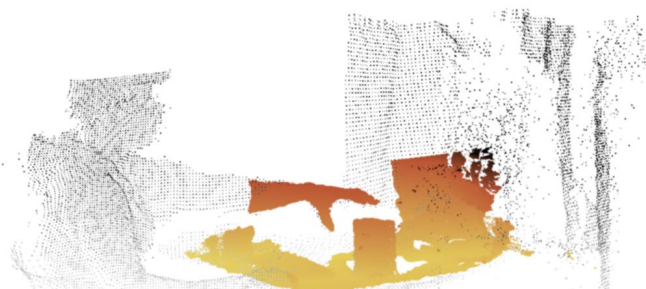
### Room state 1: *Work*



### Room state 2: *Meeting*



### Room state 3: *Coffee break*





Binary Tree



Stack



Matrix



Unbalanced Tree



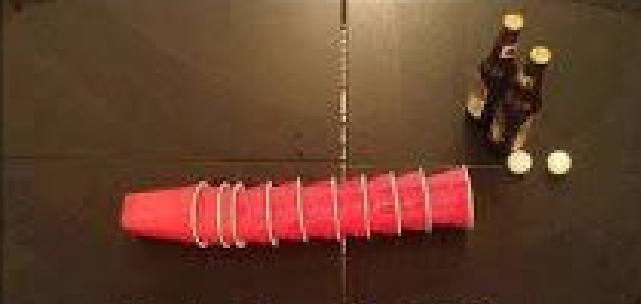
Array



Heap



Rebalanced Tree

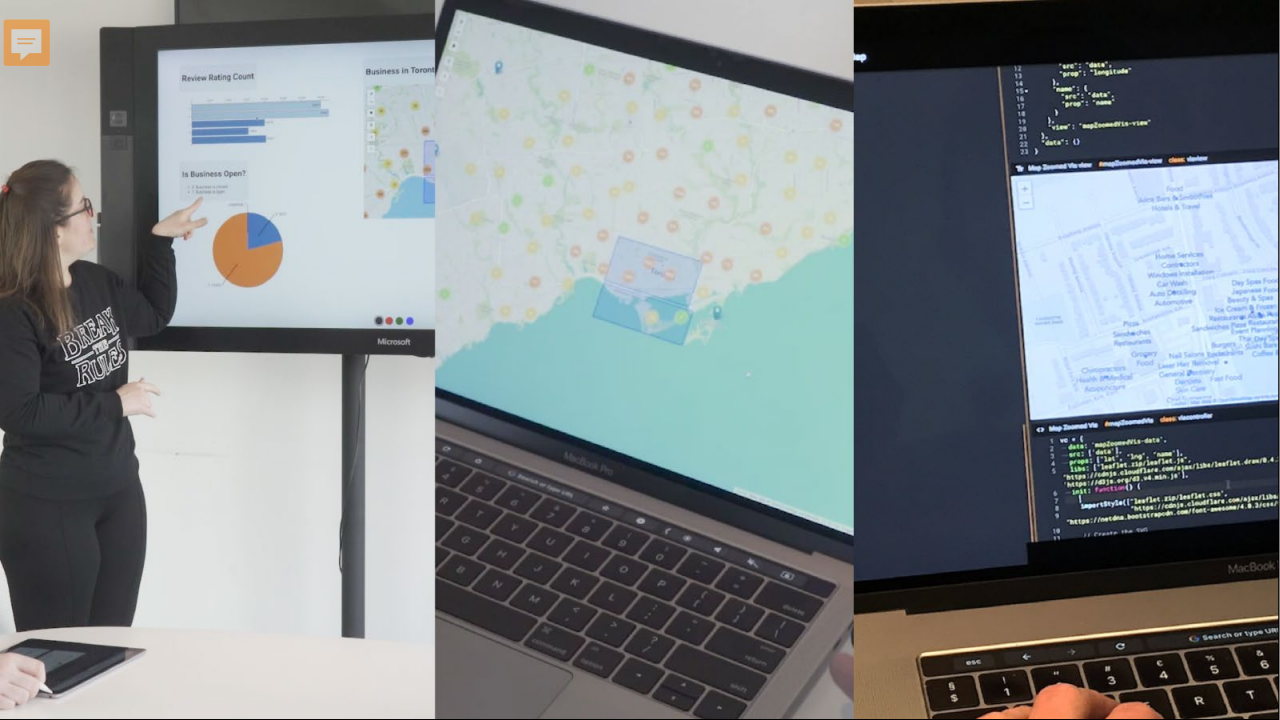


Linked List



Sparse Matrix

Data Structures and Algorithms



## A Component Model for Ubiquitous Analytics

Integrating Data-Driven Reporting  
in Collaborative Visual Analytics



$$\frac{(e, h, S) \rightarrow_{n,h} (e', h', S') \quad Z' = Z[n \mapsto S'] \quad H' = H[n \mapsto h']}{\langle n; e \rangle, (H[n \mapsto h], Z[n \mapsto S'], L, P, M) \rightarrow_h \langle n; e' \rangle, (H', Z', L, P, M)}$$

$$\frac{Z(n) = S \quad S(z) = \text{None} \quad (ip, p) \notin \text{dom}(L) \quad p \notin P(ip) \quad Z' = Z[n \mapsto S[z \mapsto \text{Some } a]] \quad L' = L[a \mapsto n] \quad P' = P[a \mapsto P(a) \cup \{p\}]}{\langle n; \text{socketbind } z a \rangle, (H, Z, L, P, M) \rightarrow_h \langle n; 0 \rangle, (H, Z', L', P', M)}$$

$$\frac{Z(n)(z) = \text{Some } from \quad m = (from, to, msg, \text{SENT}) \quad m_{id} \notin \text{dom}(M) \quad M' = M[m_{id} \mapsto m]}{\langle n; \text{sendto } z \text{ msg } to \rangle, (H, Z, L, P, M) \rightarrow_h \langle n; \text{length } msg \rangle, (H, Z, L, P, M')}$$

$$\frac{Z(n)(z) = \text{None} \quad (ip, p) \notin \text{dom}(L) \quad p \notin P(ip) \quad m_{id} \notin \text{dom}(M) \quad m = ((ip, p), to, msg, \text{SENT}) \quad M' = M[m_{id} \mapsto m]}{\langle n; \text{sendto } z \text{ msg } to \rangle, (H, Z, L, P, M) \rightarrow_h \langle n; \text{length } msg \rangle, (H, Z, L, P, M')}$$

$$\frac{Z(n)(z) = \text{Some } a \quad m_{id} \mapsto m \in M \quad from(m) = f \quad to(m) = a \quad msg(m) = b \quad state(m) = \text{SENT} \quad m' = (f, a, b, \text{RECEIVED}) \quad M' = M[m_{id} \mapsto m']}{\langle n; \text{receivefrom } z \rangle, (H, Z, L, P, M) \rightarrow_h \langle n; \text{Some } (b, f) \rangle, (H, Z, L, P, M')}$$

$$\frac{Z(n)(z) = \text{Some } a \quad \emptyset = \{m_{id} \mid m_{id} \mapsto (-, a, -, \text{SENT}) \in M\}}{\langle n; \text{receivefrom } z \rangle, (H, Z, L, P, M) \rightarrow_h \langle n; \text{None} \rangle, (H, Z, L, P, M)}$$

$$\begin{aligned} \phi_{req}(p) &\triangleq \lambda m, \exists ps, r, sp. \text{parts}(\{p\} \cup ps) * \text{is\_req}(\text{body}(m), r + 1) * \\ &\quad from(m) \Rightarrow^{\text{prot}} \phi_{coord} * p \xrightarrow{c} (r + 1, \text{WAIT}) * p \xrightarrow{p} \{\frac{3}{4}\} (r, \text{INIT } sp) * P(\text{body}(m), p) \\ \phi_{glob}(p) &\triangleq \lambda m, \exists ga, ms, ps, r, sc, sp. \{from(m) \mid m \in ms\} = ps * \\ &\quad \text{is\_global}(\text{body}(m), r) * ga = \{m \mid m \in ms \wedge \text{is\_abort}(m, r)\} * \\ &\quad \text{parts}(ps) * from(m) \Rightarrow^{\text{prot}} \phi_{coord} * p \xrightarrow{c} (r, \text{SC}) * p \xrightarrow{p} \{\frac{3}{4}\} (r, sp) * \\ &\quad \left( *_{m \in ms} \exists m_{id}, \pi. \text{is\_vote}(\text{body}(ms), r) * m_{id} \xrightarrow{m} \{\pi\} m \right) * \\ &\quad (ga = \emptyset \wedge \neg \text{is\_abort}(\text{body}(m), r) \wedge sc = \text{COMMIT} \vee \\ &\quad (ga \neq \emptyset \wedge \text{is\_abort}(\text{body}(m), r) \wedge sc = \text{ABORT})) \end{aligned}$$

$$\phi_{part}(p) \triangleq \lambda m, \phi_{req}(p)(m) \vee \phi_{glob}(p)(m)$$

$$P \triangleq \lambda p, m. \exists log, s. m = \text{"REQUEST\_"} @ s * p \xrightarrow{l} \{\frac{1}{2}\} log * p \xrightarrow{w} \{\frac{1}{4}\} log, s$$

$$Q \triangleq \lambda p, n. \exists log, s. p \xrightarrow{l} \{\frac{1}{2}\} log @ s * p \xrightarrow{w} \{\frac{1}{4}\} log, s$$

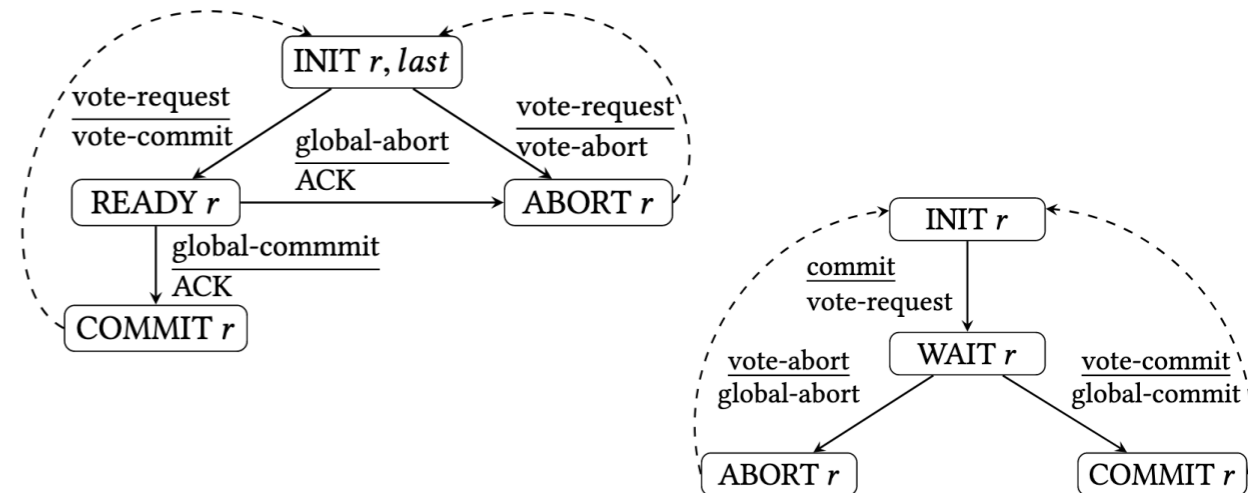
$$\frac{\text{WP-SOCKET} \quad \forall z. z \xrightarrow{s} [n] \quad \text{None} * \text{wp } \langle n; z \rangle \{ \Phi \} \quad \triangleright \text{IsNode}(n)}{\text{wp } \langle n; \text{socket} \rangle \{ \Phi \}}$$

$$\frac{\text{WP-SOCKET-BIND-DYN} \quad \forall g. z \xrightarrow{s} [n] \quad \text{Some } (ip, p) * (ip, p) \xrightarrow{r} g * (ip, p) \Rightarrow^{\text{prot}} \phi * \text{wp } \langle n; 0 \rangle \{ \Phi \} \quad \text{freePorts}(ip, \{p\}) \xrightarrow{f} A \quad (ip, a) \notin A \quad \phi \quad z \xrightarrow{s} [n] \quad \text{None}}{\text{wp } \langle n; \text{socketbind } z (ip, a) \rangle \{ \Phi \}}$$

$$\frac{\text{WP-SOCKET-BIND-STAT} \quad \forall g. z \xrightarrow{s} [n] \quad \text{Some } (ip, p) * (ip, p) \xrightarrow{r} g * \text{wp } \langle n; 0 \rangle \{ \Phi \} \quad \xrightarrow{f} A \quad \text{freePorts}(ip, \{p\}) \quad (ip, p) \in A \quad (ip, p) \Rightarrow^{\text{prot}} \phi \quad z \xrightarrow{s} [n] \quad \text{None}}{\text{wp } \langle n; \text{socketbind } z (ip, a) \rangle \{ \Phi \}}$$

$$\frac{\text{WP-SEND-TO-BOUND} \quad P \quad z \xrightarrow{s} [n] \quad \text{Some } a \quad d \Rightarrow^{\text{prot}} \phi \quad \forall m_{id}, M. m\text{Soup}(M) * m_{id} \xrightarrow{st} (a, d, s) * P \cong m\text{Soup}(M) * \triangleright \phi(a, d, s) * Q \quad z \xrightarrow{s} [n] \quad \text{Some } a * Q * \text{wp } \langle n; \text{length}(s) \rangle \{ \Phi \}}{\text{wp } \langle n; \text{sendto } z s d \rangle \{ \Phi \}}$$

$$\frac{\text{WP-SEND-TO-UNBOUND} \quad P \quad z \xrightarrow{s} [n] \quad \text{None} \quad d \Rightarrow^{\text{prot}} \phi \quad a = (ip, p) \quad \text{freePorts}(ip, \{p\}) \quad \forall p, m_{id}, M. m\text{Soup}(M) * m_{id} \xrightarrow{st} (a, d, s) * P \cong m\text{Soup}(M) * \triangleright \phi(a, d, s) * Q \quad z \xrightarrow{s} [n] \quad \text{None} * Q * \text{wp } \langle n; \text{length}(s) \rangle \{ \Phi \}}{\text{wp } \langle n; \text{sendto } z s d \rangle \{ \Phi \}}$$



# INCOMPLETENESS

ML problems are *underdetermined* (like all problems requiring induction).

- There are multiple (often infinite) allowed solutions (models) some of which might not align with the intention of the programmer.

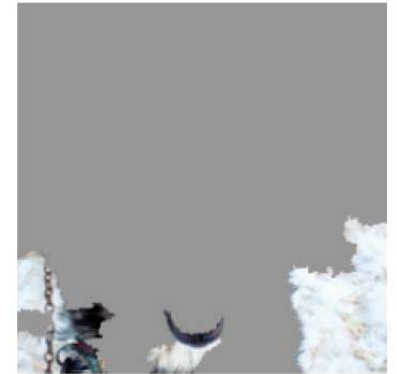
Examples:

- Training images divided into wolf and husky categories → to the model they might as well be divided into snow-in-background and not-snow-in-background images because of *insufficient* data.
- Asthma correlates with lower risk of death from pneumonia but only through a *missing* confounder (treatment).

Incompleteness can be reduced but not removed.



(a) Husky classified as wolf

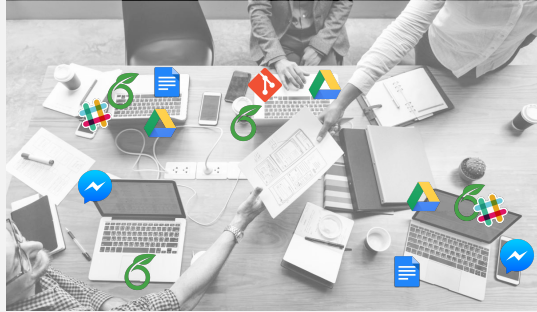


(b) Explanation

**HasAsthma(x) → LowerRisk(x)**

Rule predicting lower risk of death from pneumonia for asthmatics contrary to existing knowledge.

## Phenomenon



Behaviors

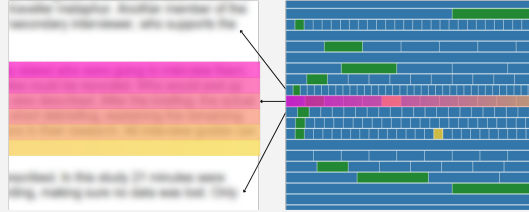


Cognitions



Sentiments

## Methodology

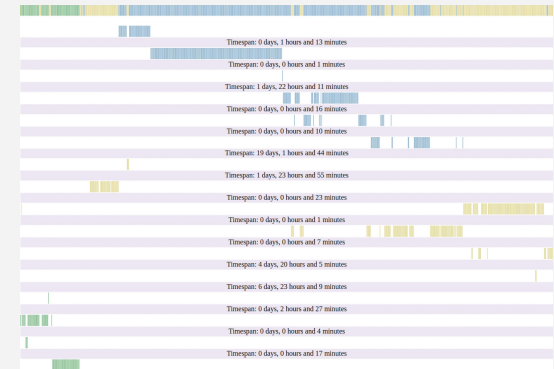


## Findings



“[You] respect each other’s sections so you don’t go and edit them.”

*(Group R15)*



# Social and Practical Functioning during Collaborative Writing

Ida Larsen-Ledet

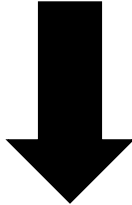
Ph.D. student

The Computer Mediated Activity group

**Node.js  
Application**

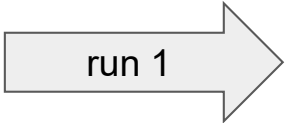


Several callbacks scheduled to run

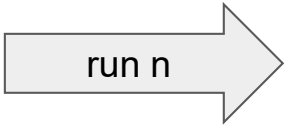


- Dynamic analysis
- Happens-before relations
- Controlled execution

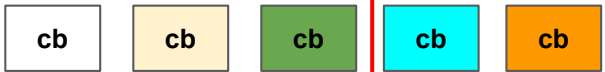
**Instrumented  
Application**



⋮



⋮



**Race  
Bug**

My research involves building better tools to reason about programming languages:

- Modern PLs are a zoo (concurrency, mutable variables, exceptions, oh my!)
- To reason about complicated programs, we need complicated tools.
- To reason about those tools, we use.... well moderately less complex math.<sup>1</sup>

Example: for concurrent code and no GC, we built a logic to prove nothing leaks.

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<sup>1</sup>I also am interested in building tools for reasoning about that math. That's a different slide though



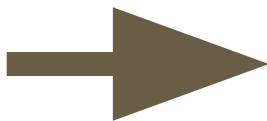
# THE INTERPLAY BETWEEN FORCE FEEDBACK AND SHAPE CHANGE



# Optimising Functional-/Stream-based programming in Java

```
public int sumEvenSquares() {  
    return IntStream.range(0, 1000000000)  
        .filter(x -> x % 2 == 0)  
        .map(x -> x * x)  
        .sum();  
}
```

Static analyses



Compiler optimisations

```
public int sumEvenSquares() {  
    int sum = 0;  
    for(int x = 0; x < 1000000000; x++)  
        if(x % 2 == 0)  
            sum += x * x;  
    return sum;  
}
```

Declarative:  
Decouples behaviour from  
implementation

Requires invocations of virtual  
functions and lambdas

Fast

No function invocations required

# VIBROTACTILE CUES FOR PROVIDING GUIDANCE IN INTERACTIVE DATA VISUALIZATION

Visual cues are often used in data visualization but can be ineffective when multiple visual cues used at the same time.

